

# Prediction-based Resource Allocation using LSTM and minimum cost and maximum flow algorithm

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# Introduction

- Research Background
- Objective

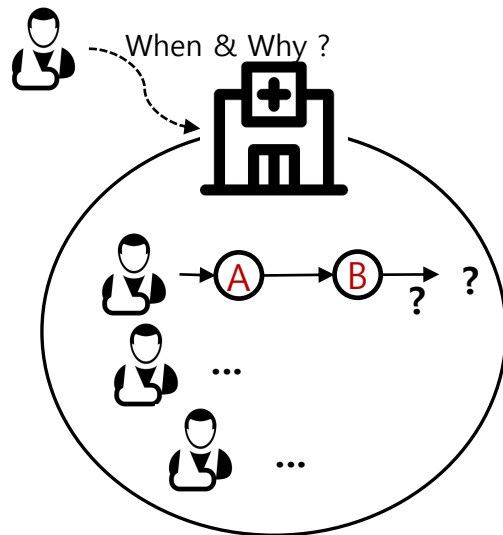
# Introduction – Research Background

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- **Resource allocation in business process management (BPM)**
  - Resource allocation in BPM **aims at allocating appropriate resources to tasks at the correct time**, to balance the demand for process executions against the availability of these resources.
  - It has been recognized as an important issue in BPM since **efficient resource allocation improves productivity, balances resource usage, and reduces execution costs**.
  - In a more general perspective, it shares commonalities with **job-shop scheduling problem in operations research**.
    - This problem finds the job sequences on machines to achieve an objective (e.g., minimizing total completion time), which is NP-hard and computationally intractable combinatorial problem.
    - There has been considerable research in the area of job shop scheduling over the past years.
      - ✓ Dispatching rules (Huang et al., 2015)
      - ✓ Shifting bottleneck heuristics (Braune et al., 2016)
      - ✓ Local Search (Kuhpfahl et al., 2016)

# Introduction – Research Background

- **Resource allocation in business process management (BPM)**
  - Among the techniques, **dispatching rules** receive massive attention from practical viewpoint since it is useful to find **a reasonably good solution in a relatively short time**.
  - However, they are applicable **only if the required parameters** such as the release time, the processing time, and the sequence of operations of jobs **are known in advance**.
  - Instead, we have **limited information** about the scheduling parameters in many circumstances.

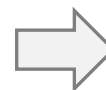


<Emergency department>

Unaware of,  
1. When and why a patient would come into the department  
2. Clinical procedures  
3. Processing time taken to finish an operation



**Non-clairvoyant Online Job Shop Scheduling Problem**

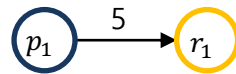


Prediction can play a key role in this problem

# Introduction – Research Background

- **Motivating example**

- Suppose we find optimal resource allocation (in terms of **total weighted completion time**) for “MRI” operation in emergency department.



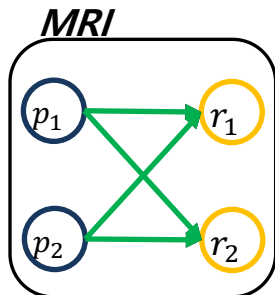
<Notation>

	$p_1$	$p_2$	$p_3$
<i>Weight</i>	1	1	10

<patient weights (Urgency)>

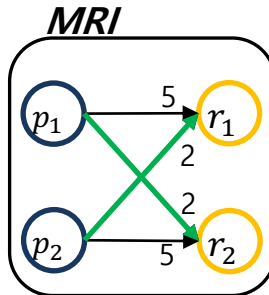
Initial Setting

At  $T = t$ ,



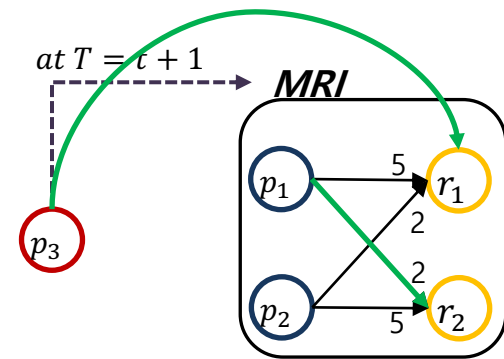
Allocation

Predicting the processing time →  
Assigning most efficient resource



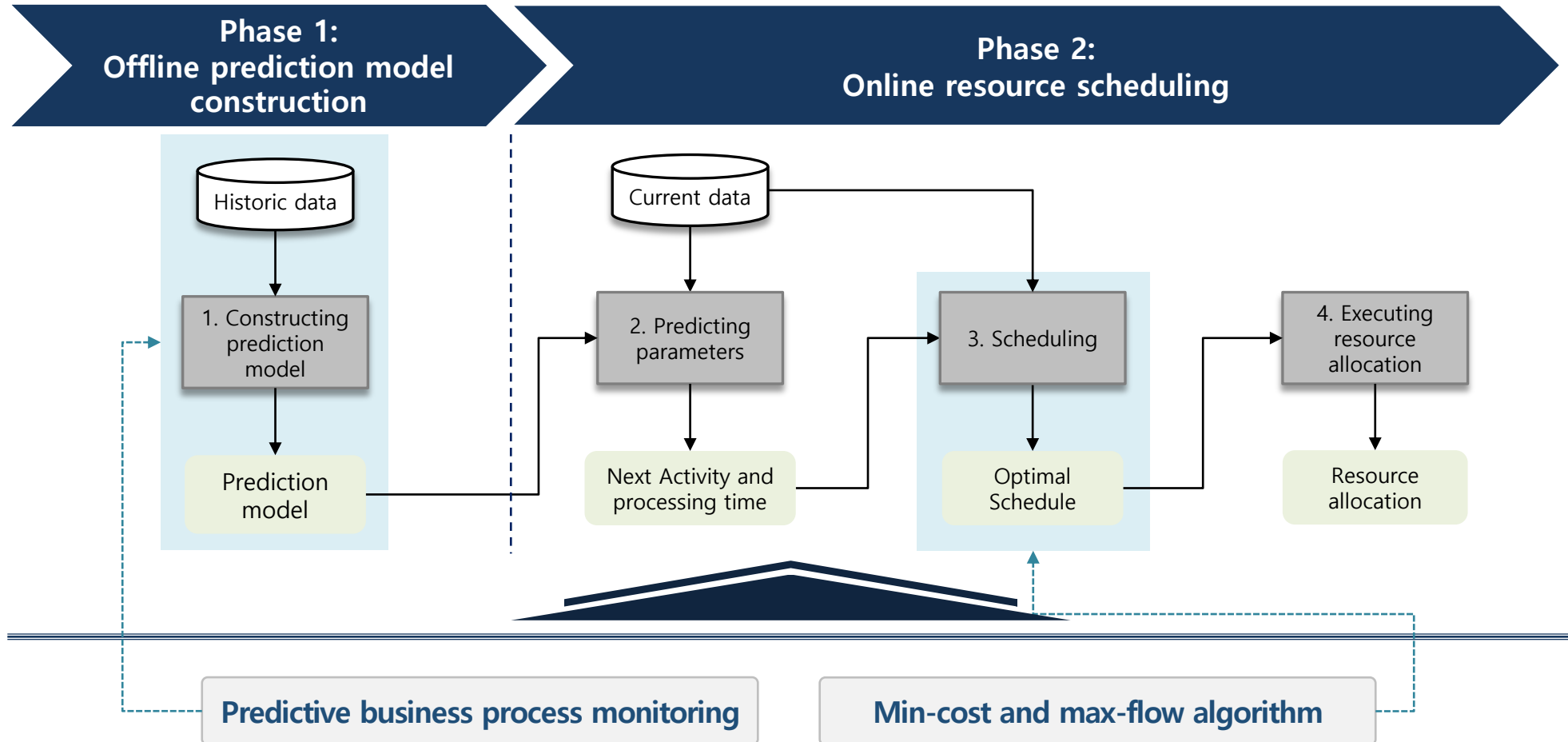
Allocation

Predicting that  $p_3$  will require “MRI” →  
Reserving  $r_1$  for  $p_3$



Allocation

# Introduction – Objective



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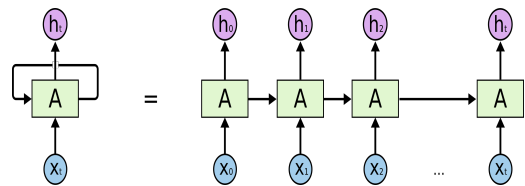
# Background

- Preliminaries
- Problem Statement
- Baseline approach



# Background – Preliminaries

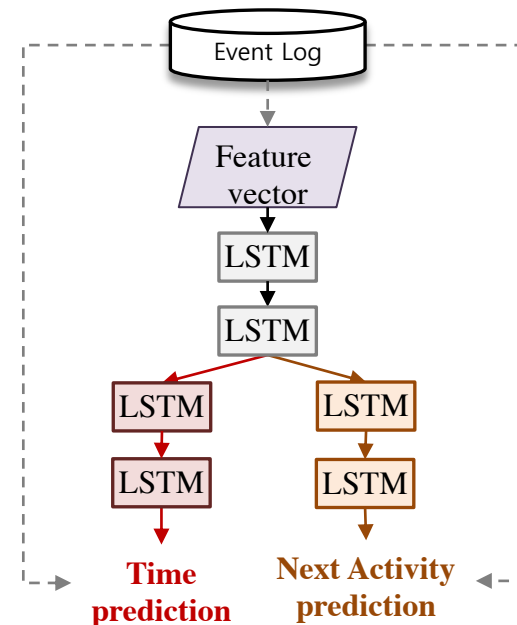
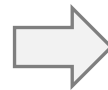
- **Predictive business process monitoring**
  - Predictive business process monitoring aims at **providing timely information** that enable **proactive and corrective actions** to improve process performance and mitigate risks.
    - Next event prediction: predicting the next event of a running instance such as **next activity**.
    - Time prediction: predicting time-related properties of a running instance such as **remaining time and processing time**.
  - Tax et al. (2017) propose an approach that predicts both the next activity and its timestamp using LSTM (Long-Short Term Memory Neural Network).



## LSTM

### (Long-Short Term Memory)

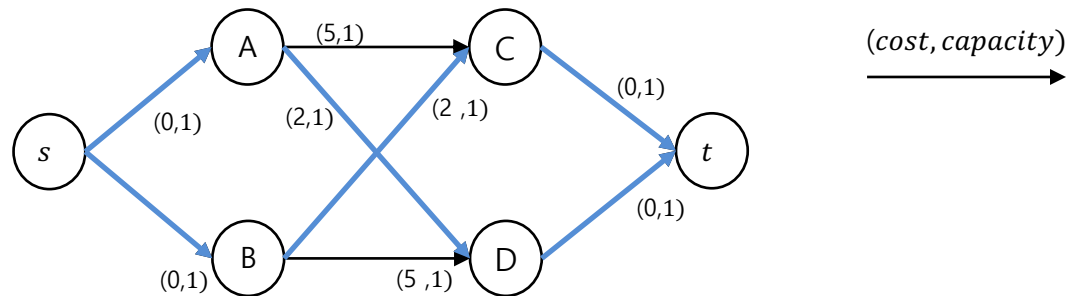
- Sequence learning tasks  
(e.g., Natural language processing (NLP) )
- Learning temporal dynamics



# Background – Preliminaries

- **Minimum cost and maximum flow problem**

- Minimum cost and maximum flow problem is a way of **minimizing the cost required to deliver maximum amount of flow possible in the network.**
  - E.g., A directed graph  $G = (V, E)$  with a source node  $s \in V$  and a sink node  $t \in V$ , where each edge  $(u, v) \in E$  has cost and capacity.



<Minimum cost and maximum flow of  $G$ >

- It can be solved in polynomial time using the network simplex algorithm.

# Background – Problem Statement

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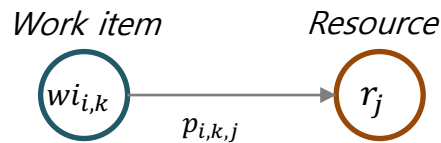
- **Non-clairvoyant Online Job Shop Scheduling Problem**

- Given a set of instances  $I$ , this problem **finds an optimal scheduling of all operations** within instances while **minimizing total weighted completion time  $\sum_i w_i C_i$** ,
  - $w_i$ : weight of  $I_i$
  - $C_i$ : difference between the finish time  $F_i$  and start time  $S_i$  of an instance  $I_i$ .
- Assumptions:
  1. **Unaware of the information** regarding an instance **except the weight** of it.
  2. Find out the **next operation of an instance** only if the instance finishes its current operation.
  3. Each operation has **a specific set of resources** with whom it needs to be processed.
  4. **Only one operation** within an instance can be processed at a given time.
  5. Once processing begins on an operation, **it cannot be stopped** until completion.

# Background – Problem Statement

## • Running Example

- Suppose there are 5 instances and 3 resources in the process.
  - $I_1, \dots, I_4$  are ready for the allocation at  $T = t \rightarrow$  We don't know the processing time.
  - $I_5$  is currently doing its 2<sup>nd</sup> operation (i.e.,  $wi_{5,2}$ ) at  $T = t \rightarrow$  We don't know the next activity (and required resource).



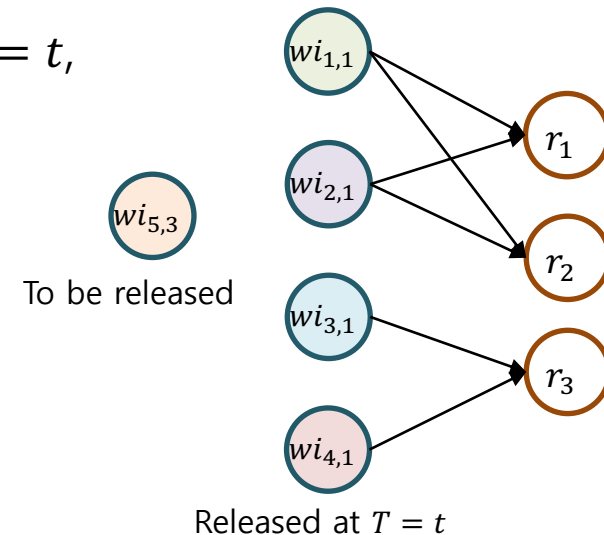
<Notation>

$\rightarrow wi_{i,k}$  ( $k^{th}$  operation of instance  $I_i$ )  
can be processed by  $r_j$   
in  $p_{i,k,j}$  (processing time)

	$I_1$	$I_2$	$I_3$	$I_4$	$I_5$
Weight	1	1	1	5	10

<Instance weights>

At  $T = t$ ,



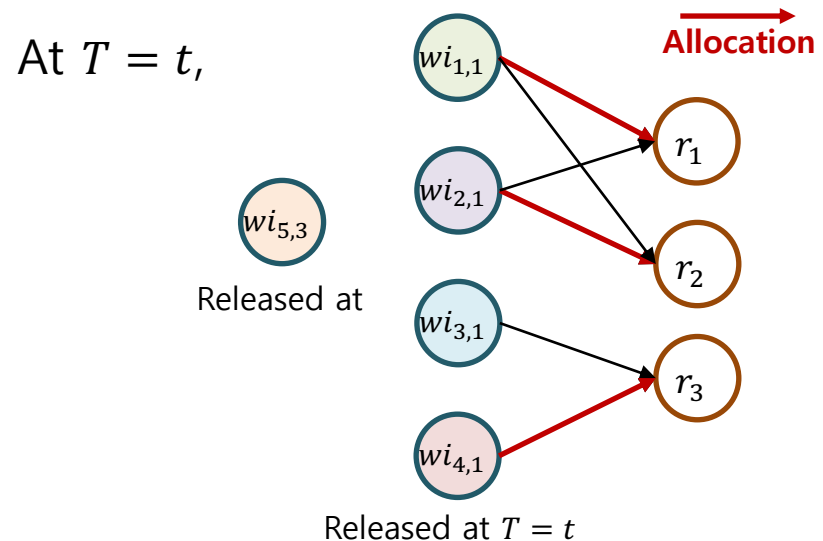
# Background – Baseline approach

- Baseline Approach (*WeightGreedy*)

1. Each work item is assigned to an available resource in a “**first come, first served**” manner.
2. If there exist conflicting demands for the same resource, the work item with **higher weight** is served first.
3. If the competing work items have the same instance weights, the **tie is broken at random**.

	$I_1$	$I_2$	$I_3$	$I_4$	$I_5$
<i>Weight</i>	1	1	1	5	10

<Instance weights>



Here

	$t$	$t+1$	$t+2$	$t+3$	$t+4$	$t+5$	$t+6$	$\sum w_i C_i$
$r_1$		$wi_{1,1}$					$wi_{5,3}$	65
$r_2$			$wi_{2,2}$					5
$r_3$		$wi_{4,1}$	$wi_{3,1}$					15

85

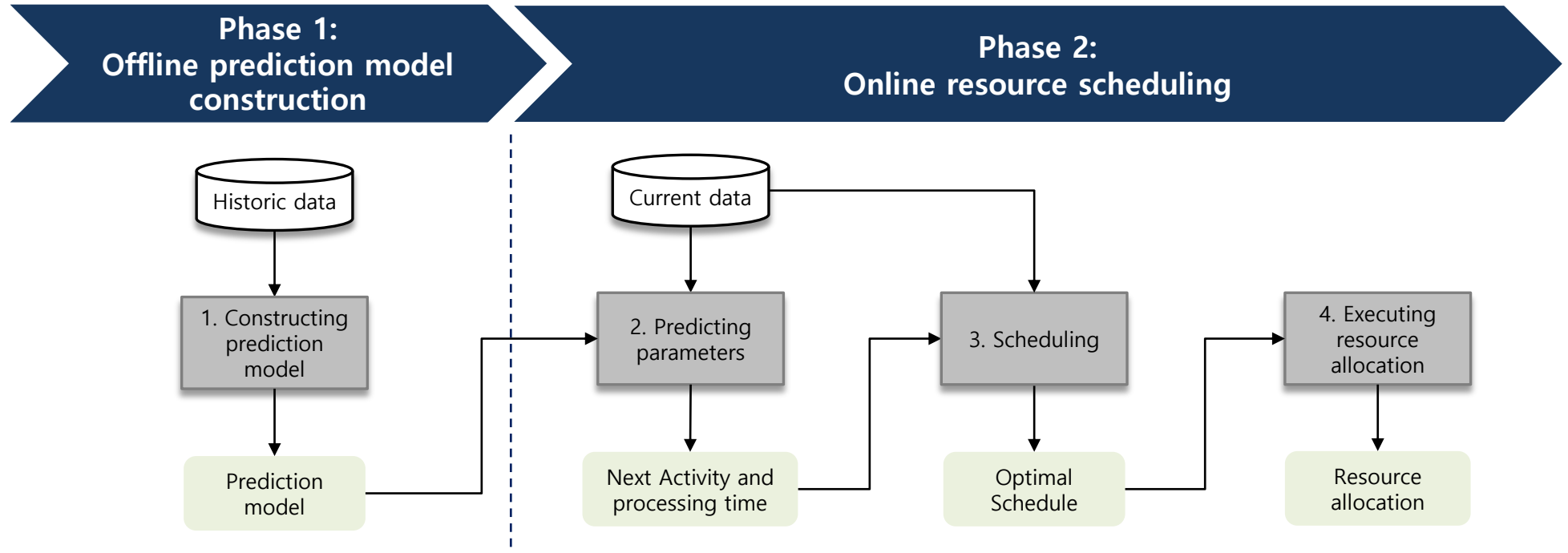
<Result of resource allocation based on *WeightGreedy*>

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# Method

- Overview
- Steps

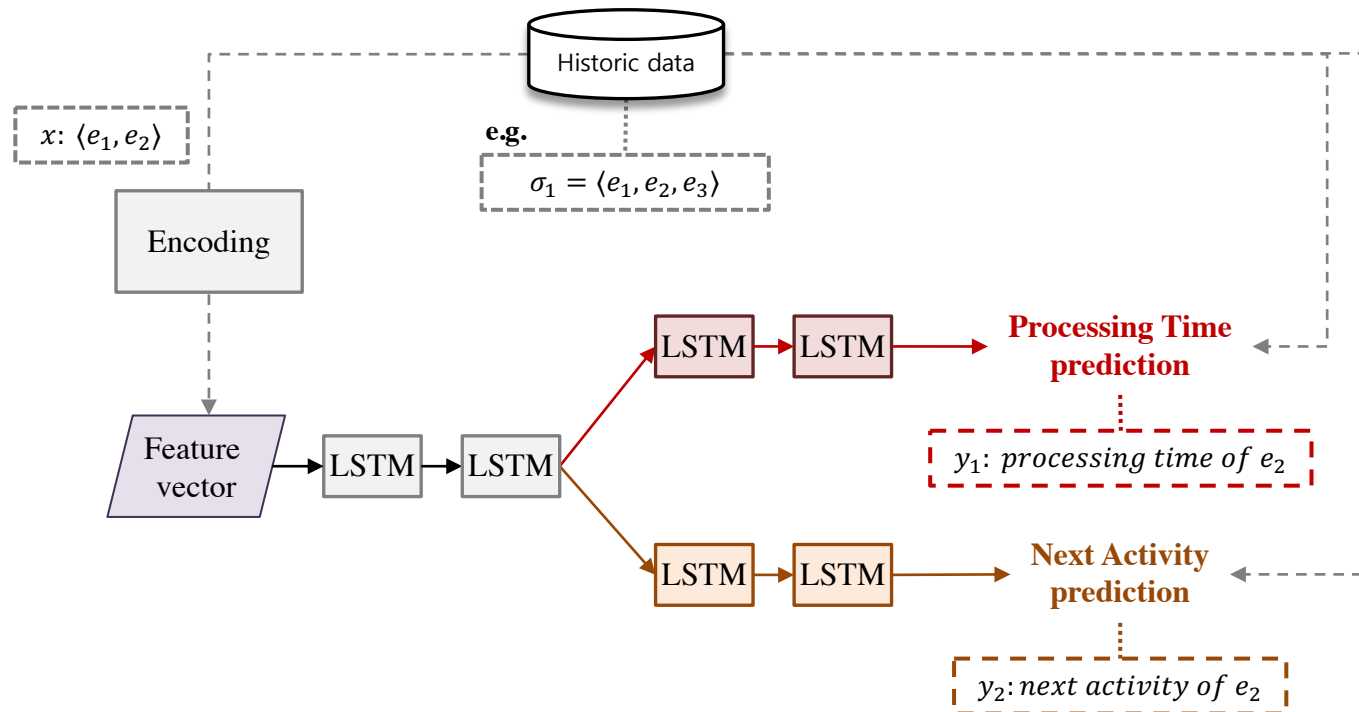
# Method – Overview



# Method – Phase 1

- **Step 1: Constructing Prediction Model**

- In this step, we aim at building a model to predict the **processing time** and the **next activity** of a running instance, which is based on LSTM (Tax et al, 2017).
- We learn the model with all traces in the historic data.
  - E.g., Training with a trace  $\sigma_1 = \langle e_1, e_2, e_3 \rangle$





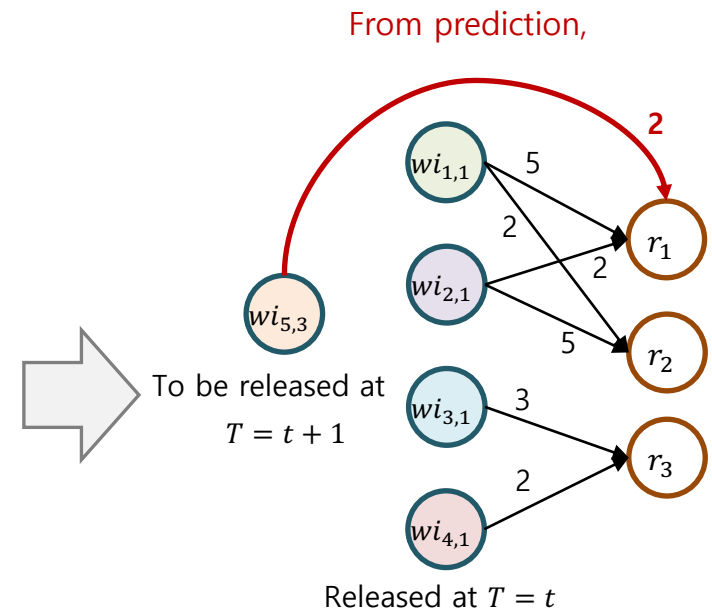
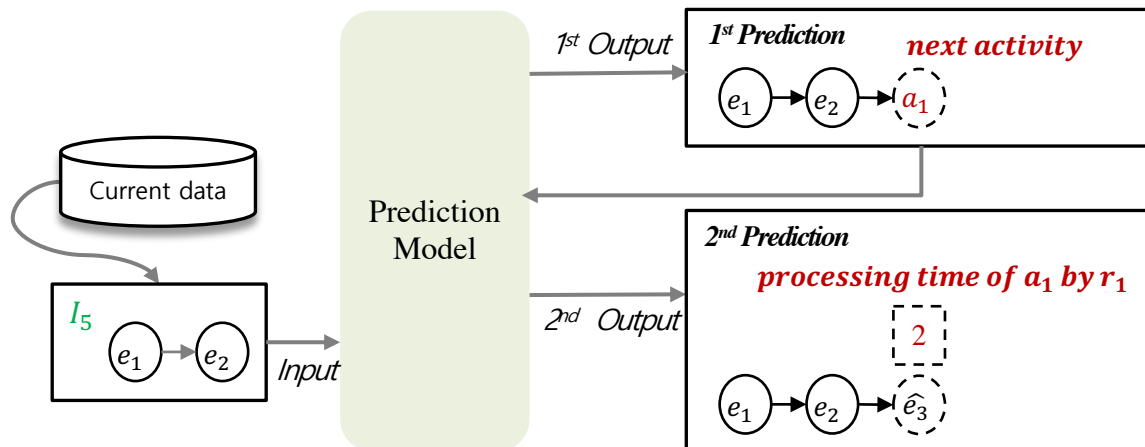
# Method – Phase 2

- **Step 2: Predicting parameters**

- Based on the prediction model we construct in the previous step, we predict the **next activity and processing time** of ongoing instances from the current data.
- We conduct **two consecutive predictions** for a running instance.
  1. Predict the next activity of it.
  2. Predict the processing time of the activity by available resources.

E.g.,

- $I_5$  is currently at its 2<sup>nd</sup> operation.
- We first predict its next activity  $a_1$
- Next, we predict the processing time of  $a_1$  by resource  $r_1$ .

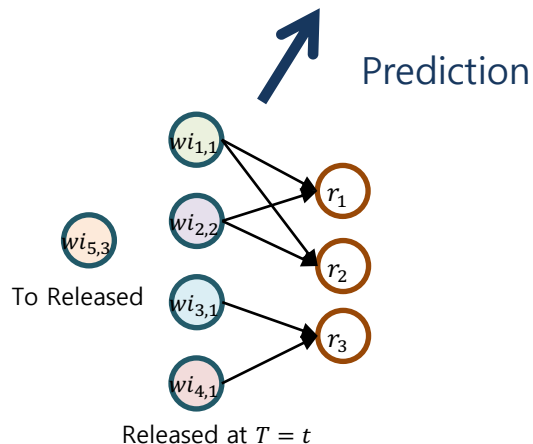
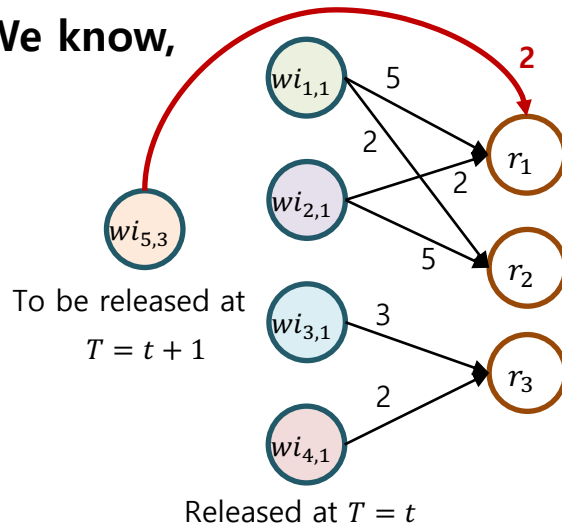


# Method – Phase 2

## • Step 3: Scheduling

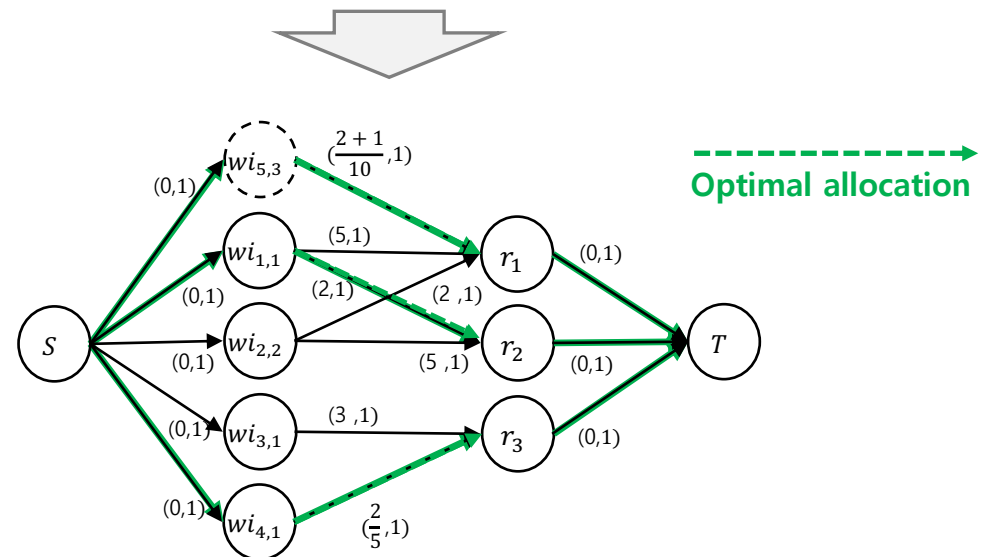
- In this step, we find an optimal scheduling by solving a min-cost max-flow network problem.

We know,



Cost function is designed to minimize total weighted completion time

1. Connect source(sink) node to  $\widehat{WI}(\widehat{R})$ . Edges have cost of 0 and capacity of 1.
2. If a work item can be processed by a resource, add edges with (*cost*, *capacity=1*).
3. Apply min-cost max-flow algorithm to find the optimal allocations.



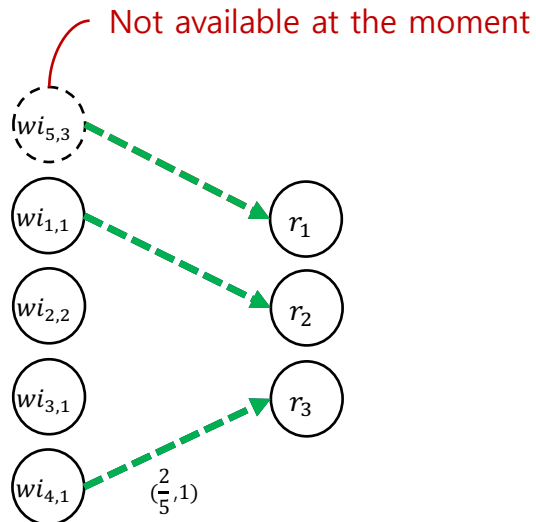
# Method – Phase 2

## • Step 4: Executing resource allocation

- In this step, we classify the optimal allocations into **executable and non-executable allocations** and then execute only the executable allocations.

- *Executable allocation* : both instance and resource are available at the moment
- *Non-executable allocation* : either instance or resource is not available at the moment

At  $T = t$ ,



Here

	$t$	$t+1$	$t+2$	$t+3$	$t+4$	$t+5$	$t+6$	$\sum w_i c_i$
$r_1$			$wi_{5,3}$			$wi_{5,3}$		65
$r_2$				$wi_{2,2}$				5
$r_3$		$wi_{4,1}$		$wi_{3,1}$				15

improve

	$t$	$t+1$	$t+2$	$t+3$	$t+4$	$\sum w_i c_i$
$r_1$			$wi_{5,3}$	$wi_{2,2}$		25
$r_2$		$wi_{1,1}$				2
$r_3$		$wi_{4,1}$		$wi_{3,1}$		15

<Result of resource allocation>

- Executable allocation
- Non-Executable allocation

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# Evaluation

- Artificial event log
- Real-life event log

# Evaluation – Artificial event log

- Experimental design

- Procedure

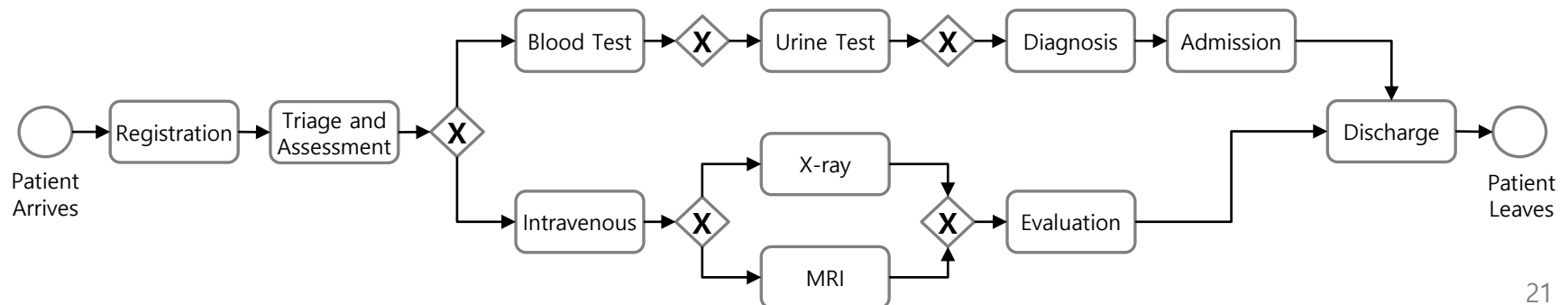
1. Design a business process and generate historic data and current data by simulating it.
2. Compare our proposed method with baseline approach in terms of **total weighted completion time** and **computation time by varying the number of instances**.

- Process description

- Emergency treatment process at a hospital with 11 activities and 25 resources
- Each resource has different skills and proficiency level.
- Patients with different weights (1~10) come into the process in a regular interval.

- Log Generation

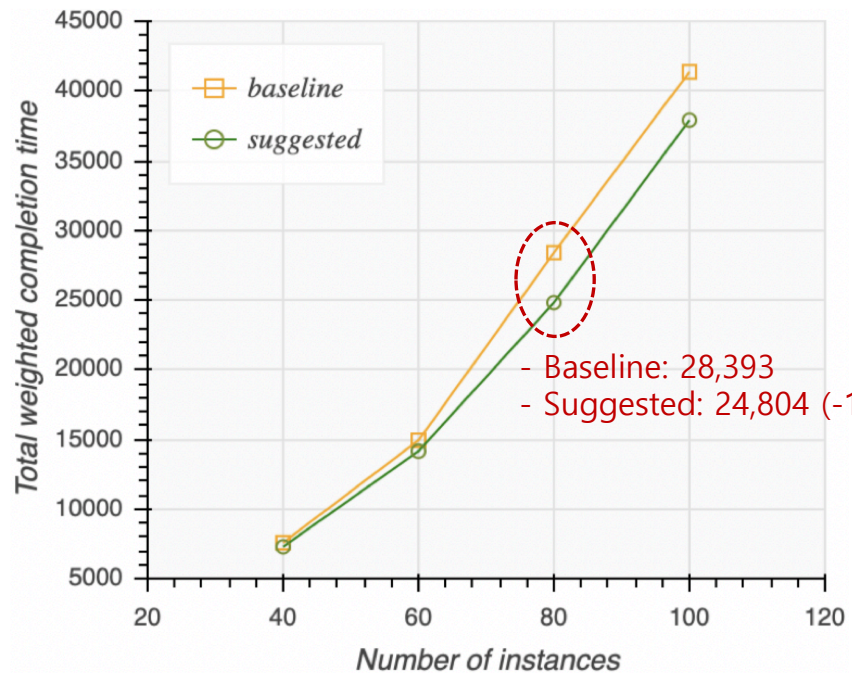
- Historic data: 7 days, 1,000 instances
- Current data: 6 hours, 40~120 instances



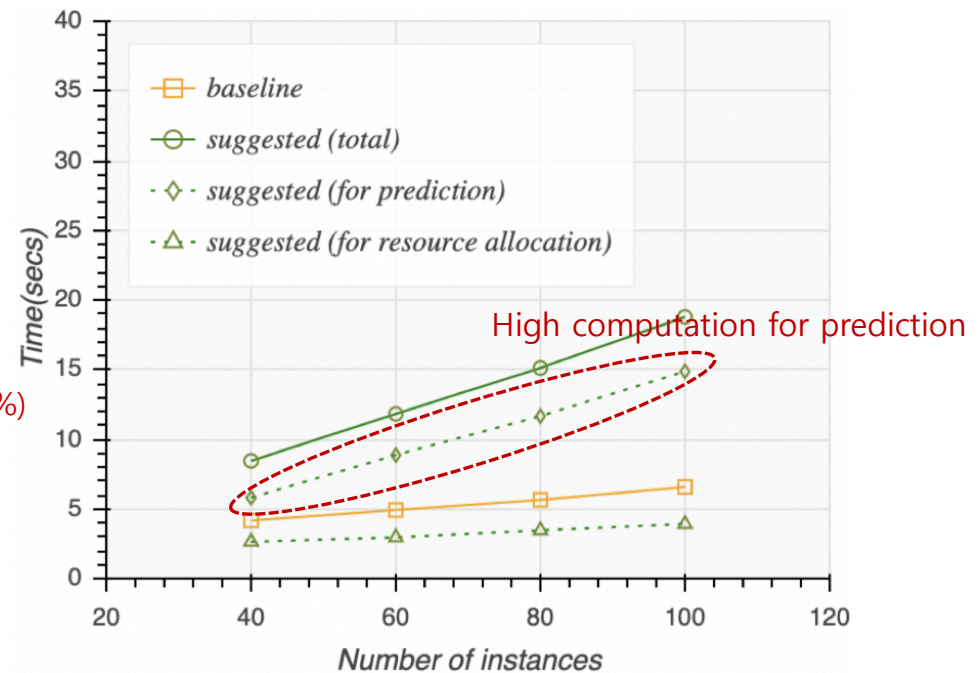
# Evaluation – Artificial event log

- Results

- Total weighted completion time and computation time, given the different number of instances.



<Total weighted completion time of varying  $||$ >



<Computation time of varying  $||$ >

# Evaluation – Real-life event log

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- **Experimental design**

- Procedure

1. Generate historic data and current data by splitting the real-life log.
2. Compare our proposed method with baseline approach in terms of **total weighted completion time and computation time**

- Process description

- Application procedure for a personal loan at a global financing organization (BPIC'12)
- 7 activities and 48 resources
- 13,087 cases and 262,200 events from Oct. 2011 to Mar. 2012
- According to the case attribute "*AMOUNT\_REQ*", we assign the weight (1~10) to each instance.

- Log split

- Historic data: events before 10<sup>th</sup> Mar. 2012
- Current data: 10<sup>th</sup> Mar. 2012
  - ✓ contains 110 instances, each conducting 3 activities on average

# Evaluation – Real-life event log

- **Results**

- Total weighted completion time and computation time.
  - Total weight completion time of the proposed method is **42 percent lower** than the one of baseline approach.
    - ✓ assigning the most efficient resources and reserving some resources for future allocation
  - The computation time is much higher in the proposed method.
    - ✓ each work item has many resource options → high computation for predicting the parameters (110.1 out of 115.6)

<Experimental result on real-life event log>

Method	Total weighted completion time	Computation time(secs)
Baseline	1479	7.6
Suggested	1038 (-42%)	115.6

For prediction: 110.1 secs  
For scheduling: 5.5 secs



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# Conclusion

- Contribution
- Limitation
- Future works

# Conclusion

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- **Contribution**

- In this paper, we suggest a **concrete method to improve a business process using results from predictive business process monitoring**.
- To this end, we adopt **the time and next event prediction technique based on LSTM** and **min-cost max-flow algorithm** to optimize online resource scheduling.
- We verify the effectiveness and efficiency of the proposed method on **both an artificial log and a real-life log**.

- **Limitation**

- Our proposed method relies heavily on the **performance of the prediction model**.
- The **computation time** is relatively higher than the baseline approach.

# Conclusion

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- **Future work**
  - We will conduct additional experiments such as **the effect of the prediction accuracy on the performance**.
  - We will extend this two-phase method to achieve **another goal** such as minimizing the potential risks in the business process **by predicting other relevant parameters and defining a relevant cost function of network arcs**.
  - Another direction for future work is to extend the proposed method by **adopting advanced dispatching techniques**.



# Q&A

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